

How to solve equations of the form

$$3^x = 44$$

$$\log 3^x = \log 44$$

$$x \log 3 = \log 44$$

$$x = \log 44 \div \log 3$$

combine into one term  
 **$\log A + \log B$**

$$\log (AB)$$

combine into one term  
 **$\log A - \log B$**

$$\log \left( \frac{A}{B} \right)$$

rewrite in terms of  $\log A$

$$\log (A^x)$$

$$x \log A$$

rearrange as  $\log ( )$   
 **$2 \log (AB)$**

$$\log (A^2 B^2)$$

**Formula for exponential growth**

$$\text{Value} = \text{Start} \times (1 + \text{change})^{\text{time}}$$

**Formula for exponential decay**

$$\text{Value} = \text{Start} \times (1 - \text{change})^{\text{time}}$$

The equation which generates  
 $\log_b y = x$

$$y = b^x$$

How to calculate the value of  
 $\log_b C$   
if b and C are known values

$$\frac{\log_{10} C}{\log_{10} b}$$

write as one log term  
 $2 \log X + \log Y$

$$\log (X^2 Y)$$

write as one log term  
 $\log_b 18 - 2 \log_b 3$

$$\begin{aligned} &= \log \left( \frac{18}{3^2} \right) \\ &= \log_b 2 \end{aligned}$$

**order to apply log rules**  
when simplifying expressions

- 1)  $x \log A = \log (A^x)$
- 2)  $\log (A) + \log (B) = \log (AB)$
- 3)  $\log (A) - \log (B) = \log \left( \frac{A}{B} \right)$

Simplify

$$\frac{2}{a} + \frac{3}{b}$$

$$\begin{aligned} &= \frac{2b}{ab} + \frac{3a}{ab} \\ &= \frac{2b + 3a}{ab} \end{aligned}$$

Simplify

$$\frac{3x^2 + x}{5x}$$

$$\begin{aligned} &= \frac{x(3x + 1)}{x \times 5} \\ &= \frac{3x + 1}{5} \end{aligned}$$

Simplify

$$(x^2 + 8x + 16)(x + 4)^{-1}$$

$$= \frac{(x + 4)\cancel{(x + 4)}}{\cancel{(x + 4)}} \\ = x + 4$$

Simplify

$$\frac{x^2 + 3x + 2}{x + 1}$$

$$= \frac{(x + 2)\cancel{(x + 1)}}{\cancel{(x + 1)}} \\ = x + 2$$

Write with no negative powers

$$\left(\frac{x^2}{2a}\right)^{-1}$$

$$\frac{2a}{x^2}$$

Expand  $(4x^3y)^2$

$$16x^6y^2$$

Simplify

$$\sqrt{25x^2y^6}$$

$$5xy^3$$

Write in terms of a power of  $x$

$$\sqrt{36x}$$

$$6x^{1/2}$$

Write with no negative powers

$$8x^{-2}$$

$$\frac{8}{x^2}$$