

Calculus Log and Exponents Practice #1

Solve:

1. $x = \log_6 200$

2. $\ln x = 2.1$

3. $e^x = 9$

4. $\log_5 (3x + 11) = 6.2$

5. $e^{2-x} = 3.1$

6. $\frac{5^{4x}}{5^{x-4}} = 199$

Solve for x in terms of k :

7. $\log_{10} (4x) = k$

8. $\ln (2x - 5) = k$

Solve:

9. $\log_{10} (x + 8) + \log_{10} (x - 5) = \log_{10} (14)$

10. $\ln (5x - 6) + \ln (3) = 2 \ln (x) + \ln (2)$

11. $\log_3 (2x + 3) - \log_3 (x - 2) = 1$

12. $\log_2 (x + 4) + \log_2 (x - 3) = 3$

13. $2 \log_2 (x) - \log_2 (x - 6) = \log_2 32$

14. $\log_3 (x^5) - 3 \log_3 (x) = 4$

Solve for x in terms of k :

15. $2 \log_4 x = \log_4 k + 1$

16. $\ln (2x - k) - \ln k = 2$

Answers: Calculus Log and Exponents Practice #1

Solve:

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|----|--------------------------------|--------------------------------|--------------------------|---------------|
| 1. | $x = \log_6 200$ | $6^x = 200$ | $x \ln 6 = \ln 200$ | $x = 2.957$ |
| 2. | $\ln x = 2.1$ | $e^{\ln x} = e^{2.1}$ | $x = e^{2.1}$ | $x = 8.166$ |
| 3. | $e^x = 9$ | $x \ln e = \ln 9$ | $x = \ln 9$ | $x = 2.197$ |
| 4. | $\log_5 (3x + 11) = 6.2$ | $5^{\log (3x + 11)} = 5^{6.2}$ | $3x + 11 = 21558.3$ | $x = 7182.4$ |
| 5. | $e^{2-x} = 3.1$ | $(2-x) \ln e = \ln 3.1$ | $2-x = 1.1314$ | $x = 0.8686$ |
| 6. | $\frac{5^{4x}}{5^{x-4}} = 199$ | $5^{3x+4} = 199$ | $(3x+4) \ln 5 = \ln 199$ | $x = -0.2370$ |

Solve for x in terms of k :

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|----|----------------------|--------------------------|----------------|-------------------------|
| 7. | $\log_{10} (4x) = k$ | $10^{\log (4x)} = 10^k$ | $4x = 10^k$ | $x = \frac{10^k}{4}$ |
| 8. | $\ln (2x - 5) = k$ | $e^{\ln (2x - 5)} = e^k$ | $2x - 5 = e^k$ | $x = \frac{e^k + 5}{2}$ |

Invalid solutions are shown struck out:

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|-----|---|----------------------------|---------------------------------------|
| 9. | $\log_{10} (x + 8) + \log_{10} (x - 5) = \log_{10} (14)$ | $(x + 8)(x - 5) = 14$ | $x = 6$ or -9 |
| 10. | $\ln (5x - 6) + \ln (3) = 2 \ln (x) + \ln (2)$ | $3(5x - 6) = 2x^2$ | $x = 6$ or 1.5 |
| 11. | $\log_3 (2x + 3) - \log_3 (x - 2) = 1$ ($1 = \log_3 3$) | $\frac{2x + 3}{x - 2} = 3$ | $x = 9$ |
| 12. | $\log_2 (x + 4) + \log_2 (x - 3) = 3$ ($3 = \log_2 8$) | $(x + 4)(x - 3) = 8$ | $x = 4$ or -5 |
| 13. | $2 \log_2 (x) - \log_2 (x - 6) = \log_2 32$ | $\frac{x^2}{x - 6} = 32$ | $x = 8$ or 24 |
| 14. | $\log_3 (x^5) - 3 \log_3 (x) = 4$ ($4 = \log_3 81$) | $x^{5-3} = 81$ | $x = 9$ or -9 |

Solve for x in terms of k :

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|-----|-----------------------------|---|--------------------------|---------------------------|
| 15. | $2 \log_4 x = \log_4 k + 1$ | $\log_4 x^2 = \log_4 k + \log_4 4$ | $x^2 = 4k$ | $x = 2\sqrt{k}$ |
| 16. | $\ln (2x - k) - \ln k = 2$ | $\ln \left(\frac{2x - k}{k}\right) = \ln e^2$ | $\frac{2x - k}{k} = e^2$ | $x = \frac{e^2 k + k}{2}$ |