Practice for L3 Equations #6

1. Solve the system of equations

x + 2y + 2z = 1 3x + 4y + 2z = 2 2x + 2y + 3z = 4

2. A printing firm charges \$63 for 5 bindings, 1000 pages and 5 inserts. It charges \$268 for 20 bindings, 800 pages and 40 inserts. It charges \$94 for 10 bindings and 1200 pages. How much would it charge for 2 bindings, 200 pages and 5 inserts?

- Four entrées, four main courses and four desserts cost \$280.
 Three entrées, three mains and two desserts cost \$195.
 Three entrées cost the same as four desserts.
 How much is a dessert?
- 4. Peter picks three numbers that add up to 46.The middle number is four-fifths of the difference between the largest and smallest.The largest number is four more than the other two numbers added together.What are the numbers?
- 5. Describe fully the nature of the system of equations below:

 $2x + y - z = 8 \qquad \qquad 3x + 4y + z = 10 \qquad \qquad x - 2y - 3z = 6$

6. Consider the following system of equations:

x + 2y + kz = 6 x + y + z = 9 3x + 4y + 2z = 12

Find k so that the system cannot be solved and explain with a full geometrical description.



Answers: Practice for L3 Equations #6

- 1. Solution: x = 2, y = -1.5, z = 1
- 2. 5b + 1000p + 5i = 63 20b + 800p + 40i = 268 10b + 1200p = 94So b = 8.2, p = 0.01, i = 2.4. Which means 2b + 200p + 5i =**\$48.40**
- 3. 4e + 4m + 4d = 280 3e + 3m + 2d = 195 3e + 0m 4d = 0Solving gives a dessert costs \$15
- 4. x + y + z = 46 $y = \frac{4}{5}(z - x)$ x + y + 4 = z x + y - z = -4 x + y + z = 46 4x + 5y - 4z = 0x + y - z = -4

Which makes the four numbers 5, 16 and 25

5. 0 2x + y - z = 8 2 3x + 4y + z = 10 3 x - 2y - 3z = 6

taking 20 - 10 - 13 gives the equation: 0 = 0 so the system is **dependent**.

There are an **infinite number of solutions**. All three **planes** mutually **intersect along a common line**.

6. ① x + 2y + kz = 6 ② x + y + z = 9 ③ 3x + 4y + 2z = 12

taking $1^{\text{(1)}} + 2^{\text{(2)}} - 1^{\text{(3)}}$ cancels out the *x* and *y* components. To do the same for the *z* component gives that $\mathbf{k} = \mathbf{0}$. Now taking the equations $1^{\text{(1)}} + 2^{\text{(2)}} - 1^{\text{(3)}}$ gives 0 = 12

This yields an inconsistent system, where there are **no solutions**. Taking each pair of planes and finding their line of intersection gives a system of **three parallel lines**.

